## Mathematics Glossary

The terms contained in this glossary are useful in the preparation for, and delivery of, instruction and assessment on the NC Extended Content Standards in mathematics. Each term has been included for at least one of two reasons. The first being that the term is needed when providing instruction on the NC Extended Content Standards, and the second is because the term is used on the NCEXTEND1 Assessment. This glossary is meant to be all-inclusive of the terms that are used from Kindergarten through high school. Synonyms are provided for several terms, which may be helpful when defining words for students.

| Term |  |
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| About | close to; almost. |
| Above | a location; higher. |
| Acute angle | an angle with a measure greater than $0^{\circ}$ and less than $90^{\circ}$. |
| Add | to combine two or more quantities to find one quantity called a total or sum. |
| Add fractions | to calculate the sum of two or more fractions; when fractions have a common <br> denominator, their sum is the fraction whose numerator is the sum of their <br> numerators and whose denominator is the common denominator (e.g., $1 / 5+$ <br> $4 / 5=5 / 5)$. |
| Addition | a mathematical operation of combining two or more numbers into a sum. |
| Addition sign (+) | a symbol (+) that shows that one number is to be added to another. |
| Additive inverse | two numbers are opposites if they are each the same distance away from zero, <br> but on opposite sides of the number line. |
| After | behind; the periods of time following an event. |
| Afternoon | the time from noon or lunchtime to evening. |


| Algebra | A systematic way of expressing generality and abstraction. <br> The systematically guided transformation of symbols. |
| :--- | :--- |
| Algebraic Equation | an equation that says two things are equal and includes one or more variables. |
| Algebraic Expression | a mathematical phrase that is written using one or more variables and <br> constants, but which does not contain a relation symbol (i.e., $<,,>, \leq, \geq,=$, and $\neq$ ) <br> (e.g., $3 y+6$ ). |
| Algebraic Thinking | using arithmetic to develop and express generalizations; identify numerical and <br> geometric patterns to describe functional relationships |
| Amount | the sum, whole, or aggregate of two or more quantities. |
| Analog clock | a clock usually with a round face, numbers $1-12$ on it, and at least two hands (a <br> short hand pointing to the hour and a long hand pointing to the minute, and <br> perhaps an additional hand for seconds). |
| Angle | a shape, formed by two lines or rays diverging from a common point (the <br> vertex). |
| Answer | the value or values that make an equation, inequality, or open sentence true. |
| Apply | 1. to use a theorem or concept to solve an algebraic, numeric, or geometric <br> problem. <br> $2 . ~ t o ~ c a r r y ~ o u t ~ o r ~ u s e ~ a ~ p r o c e d u r e ~ i n ~ a ~ g i v e n ~ s i t u a t i o n . ~$ |
| Area | a measurement of the amount of space within a closed, two-dimensional shape. <br> Area is usually measured in terms of "square units," in which one square unit is <br> the amount of space within a square that measures one unit by one unit (for a <br> given unit of length). |
| Area model | a diagram or representation to show the relative size of a fraction. |
| arithmetic operation | applying addition, subtraction, multiplication and division (,,$+- \times, \div$ ) to an <br> equation. |
| arithmetic patterns | an arrangement of numbers that helps students discover the patterns in <br> increasing and decreasing numbers. |
| Arithmetic sequence | a sequence in which successive terms exhibit a common difference (e.g., 12, 10, <br> $8,6,4 . .).$. |


| Array | a set of objects or numbers arranged in order, commonly in rows and columns. |
| :---: | :---: |
| Ascending order | an arrangement of numbers or objects in order from least to greatest or smallest to largest. |
| Associative property for addition | a mathematical property which states that the sum of three or more numbers is always the same, regardless of their grouping. This is illustrated by $a+(b+c)=$ $(a+b)+c ; 2+(3+4)=(2+3)+4$. |
| Associative property for multiplication | a mathematical property which states that the product of three or more numbers is always the same, regardless of their grouping. This is illustrated by $a$ $\times(b \times c)=(a \times b) \times c ; 2 \times(3 \times 4)=(2 \times 3) \times 4$. |
| Attend | orients to objects, people, or activity. |
| Attribute | a characteristic of an object. Attributes may include shape, size, number of sides, number of angles, texture, weight, density, etc. |
| Attribute value | a specific characteristic of an object. For example, small, medium, and large are possible values for the attribute size. |
| Balance scales | a device for weighing. It has a balanced beam and two pans. When the pans contain exactly the same mass the beam is in balance. You can place an object in one pan and standard weights or informal units in the other to find what the object weighs. |
| Bar graph | a graph that uses horizontal or vertical bars to represent numbers in a set of data. |
| Base ten blocks | blocks used to learn place value, addition, subtraction, multiplication, and division. Base ten blocks consist of cubes (ones place), rods (tens place), flats (hundreds place), and blocks (thousands place). |
| Base ten number system | a place value number system in which 10 digits, 0-9, are used to represent a number and the value of each place is 10 times the value of the place to its right; the value of any digit in the number is the product of that digit and its place value. |
| Before | in front of; earlier than; at an earlier time. |
| Below | a location; lower. |


| Benchmark Numbers | a number such as $5,10,25,50$, or 100 that can be used to help make <br> comparisons or estimates. |
| :--- | :--- |
| Between | 1. given two numbers, another number is said to be between those two <br> numbers if it is greater than the first, but less than the second. <br> 2. a location; middle value or object. |
| Big | of considerable size. |
| Calculate | to compute; to perform the indicated operation(s). |
| Capacity | the amount of space in cubic units that a three-dimensional (solid) figure <br> occupies or contains. Units, such as cubic meters (m3), cubic inches (in.3), <br> gallons (g), liters (L), and fluid ounces (fl. oz) are used to measure volume. |
| Cardinality principle | the concept that the last number counted represents the number of elements of <br> a set. |
| Category (Categories) | a class or division of people or things regarded as having particular shared <br> characteristics. |
| Cent | a unit of money equal to $\frac{1}{100}$ of 1 dollar. |
| Centimeters (cm) | a metric unit of measure for length or distance (100 cm =1 m). |
| Change | 1. (noun) money in the form of coins and/or dollars that is received when you <br> purchase an item with more money than the item costs. <br> 2. (verb) to make or become different. |
| Circle | a two-dimensional shape formed by a set of points that are equidistant from a <br> fixed point called the center. |
| Classify | classify and sort are not the same thing- place items in pre-determined <br> categories (e.g., heavy/light, big/small, rectangles/circles). |
| Clock | 1. (analog) a clock usually with a round face, numbers 1-12 on it, and at least <br> two hands (a short hand pointing to the hour and a long hand pointing to the <br> minute, and perhaps an additional hand for seconds). <br> 2. (digital) a clock on which the time is displayed numerically (e.g., 12:22). |
| Clockwise | moving in the same direction as the hands on a clock. |
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| Coin | a flat piece of metal issued by governmental authority as money (e.g., pennies, nickels, dimes, and quarters). |
| :---: | :---: |
| Column | a set of data stacked vertically. |
| Combine | to join or merge to form a single unit or substance. |
| Common attributes | the characteristics, such as shape, size, number of sides, number of angles, weight, etc., that are shared by two or more objects. |
| Common difference | the difference between each number in an arithmetic sequence. For example, the sequence $\{3,5,7,9,11 \ldots\}$ is made by adding 2 each time, and so has a "common difference" of 2 (i.e., there is a difference of 2 between each number). |
| Common ratio | the amount between each number in a geometric sequence. |
| Commutative property for addition | a mathematical property that states the sum of numbers is always the same, no matter how the addends are ordered. This is illustrated by $a+b=b+a ; 2+1=1$ +2 . |
| Commutative property for multiplication | a mathematical property that states the product of numbers is always the same, no matter how the factors are ordered. This is illustrated by $a \times b=b \times a$ (when $a$ and $b$ are real numbers); $4 \times 6=6 \times 4$. |
| Compare | 1. to state the similarities or differences between two or more objects or figures by considering their attributes. <br> 2. to determine if one number, quantity, or amount is greater than, less than, or equal to another number, quantity, or amount. |
| Compose numbers | combine quantities to make a new quantity (e.g., a set of 2 and a set of 5 when you put them together they become a set of 7 or 3 tens and 7 ones can be composed as 37). |
| Comprises | made up of. |
| Condition | the characteristic by which a shape is identified (e.g., if a shape has 4 equal side then it is a square) |
| Congruent | Exactly equal in size and shape. |
| Congruent figures | two plane or solid figures that have the same size and shape, and one can be obtained from the other by a sequence of rotations, reflections, and/or translations. |


| Connection | understand how mathematical ideas interconnect and build on one another to <br> produce a coherent whole |
| :--- | :--- |
| Consecutive | following one right after the other in order (e.g., 1, 2, 3...). |
| Construct | build; make |
| Continuous amount | a quantity of something ${ }^{2}$ that does not consist of distinct or individual parts <br> (e.g., liquid). |
| Counting | counting must include the following five elements: a) one-to-one: there must be <br> a one-to-one relation between counting words and objects; b) stable order: <br> counting words must be recited in a consistent, reproducible order; c) <br> cardinality: the last counting word spoken indicates how many objects are in the <br> set as a whole (rather than being a property of a particular object in the set); d) <br> abstraction: any kinds of objects can be collected together for purposes of a <br> count; and e) order irrelevance: objects can be counted in any sequence without <br> altering the outcome. |
| Create | cause (something) to happen as a result of one's actions. |
| Cross-Section | the shape made when a solid is cut through parallel to the base |
| Cube | a rectangular solid with exactly six congruent square faces. |
| Cubed | the product of a number multiplied by itself three times (e.g., 343 = $7^{3}$ ). |
| Cubic units | a unit for measuring volume (e.g., cubic centimeters and cubic inches); a cube <br> that measures one unit along each edge. |
| Cup | a customary unit used to measure capacity; one cup = eight ounces. |
| Data | information collected and used to analyze a particular concept or situation. |
| Data distribution | how the measurements of a set of data are clustered together, isolated from <br> each other, or spread out. |
| Day | a period of twenty-four hours as a unit of time. |
| Decade numbers | Counting by tens on the decade, 10, 20, 30, etc |


| Decimal number | decimals, like fractions, are a way of writing numbers that are smaller than one whole. Decimals are represented by a symbol called a decimal point. As you move right from the decimal point, the first number is in the tenths place and the second number is in the hundredths place. |
| :---: | :---: |
| Decimal point | a period or dot separating the ones place from the tenths place in decimal numbers or separating the dollars from cents in money. |
| Decompose numbers | divide or separate a quantity into smaller parts (e.g., 7 can be separated into 6 and 1,5 and $2,3 \& 4$ or 56 can be decomposed as 5 tens and 6 ones). |
| Decrease (decreasing) | to take away or become smaller. |
| Defining attributes of shapes | always-present features that classify a particular object (e.g., number of sides, angles, etc.). |
| Demonstrate | to show how to do something; explain. |
| Denominator | the "bottom" number of a fraction; the number that represents the total number of parts into which one whole is divided. For example, in $3 / 4$, the 4 is the denominator and indicates that one whole is divided into 4 parts. |
| Dependent events | two or more events in which the outcome of one event affects or influences the outcome of the other event(s). |
| Descending order | decreasing order; from greatest to least or largest to smallest. |
| Describe | to give details about what someone or something is like. |
| Determine | to find or come to a decision about by reasoning, or calculation. |
| Difference | the result when one number is subtracted by another number (i.e., the "answer" to a subtraction computation). |
| Different | not the same; unlike. |
| Differentiate | recognize what makes something different. Fractional part- is an equal size part of a whole object, set of objects, or array. |
| Digit | A digit is a single symbol used to make numerals. $0,1,2,3,4,5,6,7,8$ and 9 |
| Digital clock | a clock on which the time is displayed numerically (e.g., 12:22). |
| Dime | a coin with a value of 10 cents or $1 / 10$ of one dollar. |


| Direction | the line or course on which something is going. |
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| Distance | the length between two points in space. |
| Distributive property | a mathematical property that states when the sum of addends is multiplied by a <br> factor, the result is the same as multiplying each addend by the factor and <br> adding the products together. This is illustrated by $a \times(b+c)=(a \times b)+(a \times c)$. |
| Divide | split into equal parts. |
| Division | the inverse of multiplication. An operation that involves splitting a number into <br> equal parts. |
| Division sign ( $\div$ ) | a symbol ( $\div)$ that shows that one number is to be divided by another. |
| Divisor | the number by which another number is being divided - usually singular. |
| Dollar | currency that is worth 100 cents. |
| Dot plot | a method of visually displaying a distribution of data values where each data <br> value is shown as a dot or x mark above a number line. Also known as a dot plot. |
| Endpoint | a point at either end of a line segment or the beginning point of a ray. |
| Equal | the same amount or value (i.e., $3 \times 2$ and 10 -4 are equal in value) |
| Equal Share | having the same quantity, measure, or value as another part. |
| Equal to/Equal sign (=) | a symbol (=) that means two things have the same amount, size, number, or <br> value. |
| Equality | a relationship between two quantities or, more generally two mathematical <br> expressions, asserting that the quantities have the same value, or that the <br> expressions represent the same mathematical object |
| Equally Distribute | something that is split equally between people, groups, sets, or categories. |
| Equally likely | all events, or outcomes, have the same chance of occurring. |
| Equation | a mathematical sentence stating that two expressions are equal (e.g., $5+n=$ <br> $12)$. |
| Equivalent | equal in value or amount |
| Equivalent expressions | two expressions (numerical or otherwise) in which one expression can be <br> obtained from the other using the properties of operations, such as the <br> commutative, associative and distributive properties, as well as by representing <br> numbers in the expressions in different but equivalent forms. |


| Even number | 1. a whole number that is a multiple of two. <br> 2. the same number of objects in each group. |
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| Event | a set of one or more outcomes in a probability experiment. For example, given a <br> number cube with the numbers one through six on the faces, the rolling of an <br> even number is an event. |
| Exponent | a small number written to the right and above a base number signifying how <br> many times the base number is to be multiplied to itself. |
| Expression | a mathematical representation containing numbers, variables, and operation <br> symbols; an expression does not include an equality or inequality symbol. |
| Extend a pattern | to use the pattern rule to decide the numbers (or shapes) that would come next <br> in the sequence (or pattern). |
| Face | a plane surface of a three-dimensional figure. |
| Fact family | a set of facts, each of which relates the same three numbers through addition <br> and subtraction or through multiplication and division (e.g., 3 + 4 $=7,4+3=7,7$ <br> $-4=3,7-3=4)$. |
| Factor | the numbers that are multiplied together to get a product. |
| Fahrenheit ('F) | a temperature scale based on 32 ${ }^{\circ}$ as the freezing point of water and 212 ${ }^{\circ}$ as the <br> normal boiling point of water. |
| Fair Share | an amount divided equally. |
| Few | a small number, opposite to many. |
| Figure | a shape that only has two dimensions (such as width and height) and no <br> thickness. |
| First Quadrant | a 2-dimensional graph, Cartesian plane, includes negative and positive values of <br> both x and y. This graph is divided into four quadrants, or sections, based on <br> those values. The first quadrant is the upper right-hand corner of the graph, the <br> section where both x and y are positive. |
| Flip | the transformation of a figure that produces the mirror image of the original <br> figure. As a result of the transformation, the line over which the reflection <br> occurs becomes a line of symmetry. Informally, a reflection can be thought of as <br> a "flip" of the original figure. |
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| Foot (ft) | a customary unit of measure for length or distance; $1 \mathrm{ft} .=12$ in. |
| :--- | :--- |
| Formal units | all customary and metric units of measure. |
| Formula | a mathematical statement, equation, or rule that shows a relationship between <br> two or more quantities. |
| Fourths | a whole divided into four equal parts. |
| Fraction | a number in the form a/b where a is called the numerator and b is called the <br> denominator. A fraction names a part of a whole or a part of a collection. |
| Function | 1. two sets, an input set and an output set, and a rule that assigns to each input <br> exactly one output. ${ }^{\prime}$ <br> 2. a relationship between two sets of numbers or other mathematical objects <br> where each member of the first set is paired with only one member of the <br> second set. Functions can be used to understand how one quantity varies in <br> relation to (is a function of) changes in the second quantity. For example, there <br> is a functional relationship between the price per pound of a particular type of <br> meat and the total amount paid for ten pounds of that type of meat. |
| Function rule | the rule that assigns to each input exactly one output, where one quantity <br> determines another. For example, if you are given a table of $x$ - and $y$-values, the <br> function rule will describe how the ordered pairs are related to each other in the <br> form of an equation [e.g., $f(x)=x+2$ ]. |
| Function table | a table used to represent the relationship between two values; a table of <br> ordered pairs that may follow a rule that tells how the one value is related to the <br> other value. |
| Gallon | a customary unit used to measure capacity; one gallon = four quarts. |
| Geometric Figure | any point, line, segment, ray, angle, polygon, curve, plane, surface, solid, etc. |
| Geometric Sequence | a sequence of numbers that follow a pattern in which there is a constant ratio <br> (multiplying or dividing) between terms. |
| Geometric Shape | geometric information that still remains there even if scale, orientation, location <br> and reflection are displaced from a particular geometrical object. |


| Geometry | the branch of mathematics that deals with the measurement, properties, and <br> relationships of points, lines, angles, planes, and two- and three-dimensional <br> figures. |
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| Graph | a drawing or diagram showing a numerical relationship or displaying data. |
| Graphical Representation | using symbols such as lines, bars, pie slices, or dots to depict the data |
| Greater than (>) | a relationship showing that the first term or expression has a value larger than <br> the second term or expression (e.g., $5+3>5-2$ and $2 x-4<18)$. |
| Group | a number of individuals or objects that are assembled together or that have <br> some unifying relationship. |
| Growing patterns | patterns in which the numbers increase, and the amount added changes each <br> time in a predictable way. |
| Half | fifty percent of a whole; one of two equal parts. 35 |
| Half hour | a period of time lasting 30 minutes. |
| Halves | fifty percent of a whole; one of two equal parts. |
| Heavy | of great weight; difficult to lift or move. |
| Height | the measurement from base to top or (of a standing person) from head to foot. |
| Histogram | a graph that uses horizontal or vertical bars to represent numbers in a set of <br> data. |
| Horizontal axis | the horizontal axis of a coordinate grid. |
| Hour (hr) | a unit used to measure time, $1 / 24$ of a day; 1 hour $=60$ minutes. |
| Hour hand | the shorter hand on an analog clock. |
| Hundred chart | a $10 \times 10$ grid representing the numbers from 1 to 100 in rows and columns of <br> ten. |
| Hundreds | the numbers between 100 and $999 ; ~ t h e ~ p l a c e ~ t o ~ t h e ~ l e f t ~ o f ~ t h e ~ t e n s ~ p l a c e, ~ w h i c h ~$ <br> is 10 times 10. |
| Hundreds place | the place value located three places to the left of the decimal point in a number; <br> a digit in the hundreds place has a value of 100 times the value of the digit. |
| Hundredths | one of 100 equal parts; two digits to the right of a decimal point. |
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| Identify | to recognize or distinguish. |
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| Impossible | no chance of an event happening. |
| Inch (in) | a customary unit for measuring length or distance; 12 inches $=1$ foot; roughly <br> equivalent to the distance from the end of one's thumb to the first joint. |
| Increase (increasing) | to become/becoming larger in size or quantity. |
| Independent events | two or more events, in which the outcome of one event does not influence or <br> affect the outcome of the other event(s). |
| Inequality | a mathematical sentence that contains an inequality symbol (i.e., $>,<, \geq, \leq$, or $\neq 7)$. <br> It compares two quantities. The symbol $>$ represents greater than; the symbol $<$ <br> represents less than; the symbol $\geq$ represents greater than or equal to; the <br> symbol $\leq$ represents less than or equal to; and the symbol $\neq$ represents not <br> equal to (the symbol $\neq$ is often used to express which values are not available to <br> be used for a particular expression or equation). |
| Informal unit | any tangible item that can be used to measure something (e.g., paper clips, <br> straws, pencils, cotton balls). |
| Input/output table | a table used to represent the relationship between two values; a table of <br> ordered pairs that may follow a rule that tells how the one value is related to the <br> other value. |
| Inside | situated within the confines of (something); within. |
| Interpret | to give or provide the meaning of; to explain. |
| Intersecting lines | two lines that cross at one point. |
| Interval | what is between two points or values. |
| Key | a table for decoding or interpreting; a notation that explains something, such as <br> the value of each symbol or picture on a picture graph. |
| Label | a descriptive unit. |


| Length | 1. the distance along a line or curve from one point to another; the distance can <br> be measured with a ruler or tape measure. <br> 2. the distance from one "end" to another of a two- or three-dimensional figure. <br> For example, the length of a rectangle usually refers to the length of the longer <br> side. |
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| Less | smaller; fewer. |
| Less than (<) | a relationship showing that the first term or expression has a value smaller than <br> the second term or expression (e.g., $2<3$ or $-5<-1)$. |
| Light | having little weight: not heavy. |
| Likelihood | the chance that an event will occur. |
| Line | an infinite set of points in opposite directions forming a straight path; it has only <br> one dimension, length. |
| Line plot | a method of visually displaying a distribution of data values where each data <br> value is shown as a dot or $x$ mark above a number line. Also known as a dot plot. |
| Line segment | a line segment is a part of a line that is bounded by two distinct end points and <br> contains every point on the line between its endpoints. |
| Linear equation | an equation of the form $y=m x+b$, where $m$ and $b$ can be any real number. <br> When the ordered pairs $(x, y)$ that make the equation true for specific assigned <br> values of $m$ and $b$ are graphed, the result is a straight line. |
| Linear function | a function whose graph is a line that is not parallel to the vertical axis and has a <br> constant rate of change. . epresented by an equation in the form of $y=m x+b ;$ <br> when graphed, the coordinates provided will form a straight line. |
| Linear function graph | the graph of a linear function that results in a straight line. |
| Long (longer; longest) | extending, lasting, or totaling a number of specified units; compare lengths of <br> lines, shapes, or objects. |
| Long hand | the longer hand on an analog clock; the hand on an analog clock that tells the <br> minutes. |
| Magnitude | the size of a mathematical object, a property which determines whether the <br> object is larger or smaller than other objects of the same kind |


| Manipulatives | physical objects that can be used to help solve mathematical problems (e.g., <br> tangrams, base ten blocks, number cubes, cards, rulers, counters, pattern <br> blocks, cubes). |
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| Mass | the quantity of matter in an object, often confused with weight. Mass is <br> commonly measured by how much something weighs. But weight can change <br> for different locations (such as on the moon) while the mass stays the same. |
| Match | 1. (noun) a similar or complementary pair. <br> 2. (verb) put (someone or something) together with someone or something else. |
| Mathematical problem | a problem that can be represented, analyzed, and solved using the methods of <br> mathematics. |
| Mathematical reasoning | applying mathematical techniques, concepts, and processes, either explicitly or <br> implicitly. |
| Mathematical sentence | a mathematical statement that is either an equation or an inequality. A number <br> sentence is composed of expressions, but it is not an expression. When written, <br> a number sentence always contains a relation symbol (e.g., $=, \leq,>)$. |
| Mayer's Cognitive Processes in Problem | 1. Translating - converting sentence into mental representation <br> Solving Integrating - building a mental model of the problem situation <br> 3. Planning - devising a plan for how to solve the problem <br> 4. Executing - carrying out the plan |
| Mean | a measure of center for a set of numerical data, computed by adding the values <br> in a list and then dividing by the number of values in the list. ${ }^{15}$ For example, for |
| the data set $\{3,6,8,11\}$, the mean is 7. |  |


| Measurement unit | a standard amount or quantity. Common examples are inches (in.), feet (ft), <br> ounces (oz), grams (g), minutes (min), hours (hr), etc.52 |
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| Meter stick | a ruler one meter long (usually marked off in centimeters and millimeters). |
| Mile (mi) | a customary unit of measure for length or distance; 1 mile $=5,280$ feet. |
| Miles per hour (mph) | a unit of speed, and a ratio comparing distance (in miles) and time (in hours). |
| Minuends | a quantity or number from which another is to be subtracted. |
| Minus sign (-) | a symbol ( - ) that is read as "minus" or "take away" to represent subtraction. |
| Minute hand | the longer hand on an analog clock; the hand on an analog clock that tells the <br> minutes. |
| Minutes | 1. a unit used to measure time; 1 minute $=1 / 60$ of an hour. <br> 2. each degree can be divided into 60 equal parts, called minutes. |
| Missing value | a value omitted from an equation that is needed to make the equation true <br> [e.g., $(2 \times 3) \times 5=2 \times(3 \times \square$ $)]$. |
| Model | any object, picture, or graphic that represents a mathematical concept or <br> relationship (i.e., the tens-frame with objects can model the quantity of 1-10 <br> and provide a framework for comparison). |
| Money | a medium of exchange, a measure of value, or a means of payment. |
| More | greater in number. |
| Morning | the period of time between sunrise and noon. |
| Multiplication | a mathematical operation of combining groups of equal amounts; repeated <br> addition; the inverse of division. For example, 4 multiplied by 3 is equivalent to 4 <br> $+4+4$. |
| Multiplication sign ( $\times$ ) | a symbol ( $\times$ ) written between two numbers to show that one number is to be <br> multiplied by the other. |
| Multiply | the processes by which a number is added to itself a specified number of times. |
| Negative number | the opposite of a positive number; a number to the left of zero on a horizontal <br> number line (i.e., any number less than 0$).$ |
| Next | coming immediately after the present one in order, rank, or space. |
| Nickel | a coin with a value of 5 cents or $1 / 20$ of a dollar. |


| Night | the period of darkness in each twenty-four hours. |
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| Non-standard unit | any tangible item that can be used to measure something (e.g., paper clips, <br> straws, pencils, cotton balls). |
| Number | 1. the concept of an amount, quantity, or how many items there are in a <br> collection. <br> 2. (cardinal numbers) count the number of objects in a set; (e.g., a triangle has <br> three sides). <br> 3. (ordinal numbers) indicate the position of an object in a sequence (e.g., <br> second in a race). <br> 4. (nominal numbers) label objects (e.g., room 1, room 2, etc.). |
| Number chart | a $10 \times 10$ grid representing the numbers from 1 to 100 in rows and columns of <br> ten. |
| Number cube | a cube with a number indicated on each of the six sides. |
| Number line | a graph that represents the real numbers as ordered points on a line. A number <br> line may be either horizontal (left and right) or vertical (up and down). Starting <br> at zero, the positive numbers progress to the right (or up) and the negative <br> numbers progress to the left (or down). |
| Number sense | the understanding of number size (i.e., relative magnitude), number <br> representations, number operations, referents for quantities, and measurement <br> used in everyday situations. |
| Number sentence | a mathematical statement that is either an equation or an inequality. A number <br> sentence is composed of expressions, but it is not an expression. When written, <br> a number sentence always contains a relation symbol (e.g., $=, \leq,>$, $).$ |
| Number sentences | a group of numbers that includes a mathematical operation -- think of addition, <br> subtraction, multiplication, or division -- along with a less than (<), greater than <br> (>), or an equal sign (=) (i.e., $2+2=4$ ). |
| Numeral | a symbol expressing a number (1, 2, 3, etc.) |
| Numeration | an act or instance of or the process or result of numbering or counting |
| Numerator | the number above the fraction bar that indicates the number of parts of the <br> whole in a rational number. For example, in 3/4, the 3 is the numerator. |


| Numeric pattern | an arrangement of numbers that repeat or that follow a specified rule. |
| :--- | :--- |
| O'clock | used to specify the hour when telling time. |
| Object | a material item that can be seen and touched. |
| Obtuse angle | an angle with a measure greater than $90^{\circ}$ and less than $180^{\circ}$. |
| Odds | the chance that an event will occur. Probabilities can be described as likely, if <br> the event will most probably happen; certain, if the event will definitely happen <br> (a probability equal to 1); impossible, if the event cannot happen or (a <br> probability equal to 0); unlikely, if there is little chance that the event will <br> happen. A probability can also be expressed as a fraction (e.g., 3/12). |
| One-step problem | a word problem, equation, or inequality that can be solved in one step. |
| One-to-one correspondence | match groups of equally numbered items |
| Ones | groups of one thing. |
| Ones place | the place value located one place to the left of the decimal point in a number; it <br> shows how many ones are in a number. |
| Operand | The quantity, size, or data that will change when a mathematical operation is <br> applied. |
| Opposite | two numbers are opposites if they are each the same distance away from zero, <br> but on opposite sides of the number line. |
| Order | the arrangement of people or things in relation to each other according to a <br> particular sequence, pattern, or method. |
| Ordered pair | a set of two numbers named in an order that matters; represented by ( $x, y$ ) such <br> that the first number, $x$, represents the $x$-coordinate and the second number, $y$, <br> represents the $y$-coordinate when the ordered pair is graphed on the coordinate <br> plane; each point on the coordinate plane has a unique ordered pair associated <br> with it. |
| Ordering | the process of arranging objects or numbers to show a progressive increase or <br> decrease of an attribute. |
| Orientation | the relative position or direction of something. |


| Origin | the point at which the $x$-and $y$-axes (horizontal and vertical axes) intersect on a <br> coordinate plane. The origin is described by the ordered pair ( 0,0 and serves as <br> a reference point so that all the points on the plane can be located by ordered <br> pairs. |
| :--- | :--- |
| Ounce (oz) | a customary unit used to measure mass; 1 ounce $=1 / 16$ pound; 16 ounces $=1$ <br> pound. |
| Outcome | the result or one of the possible events in a probability experiment. For <br> example, when tossing a fair coin there are two possible outcomes, heads or <br> tails. |
| Outside | situated on or near the exterior or external surface of something; situated or <br> moving beyond the confines or boundaries. |
| Pair | two of something. |
| Pan Balance | an instrument that is used to weigh objects or to compare their weights. |
| Parallel lines/line segments | two lines that do not intersect or touch each other at any point no matter how <br> far they are extended. |
| Part | a separate piece or unit of something; a piece that combines with other pieces <br> to form the whole of something. |
| Part-part-whole | a concept underlying the operations of addition and subtraction. Addition <br> involves joining two or more parts to make a total, subtraction involves finding <br> the "missing" part. |
| Partition | the process of dividing shapes or quantities, usually into equal parts. |
| Pattern unit | the portion of a pattern that is repeated. For example, AAB is the core unit in <br> the pattern AABAABAAB. |


| Patterns | 1. a sequence of objects, shapes, or numbers that repeat or change in a regular <br> manner. <br> 2. (growing) patterns in which the numbers increase, and the amount added <br> changes each time in a predictable way. |
| :--- | :--- |
|  | 3. (numeric/symbolic) an arrangement of numbers that repeat or that follow a <br> specified rule. <br> 4. (pictorial) a pattern using symbols, shapes, designs, and pictures (e.g., $\Delta \Delta \Delta 0$ <br> $\Delta \Delta \Delta \Delta)$. |
|  | 5. (recursive) a pattern in which each number is found from the previous <br> number by repeating a process. <br> 6. (repeating) a pattern that is cyclical in nature, with each cycle repeating <br> elements in the same order. |
| 7. (shrinking) patterns in which the numbers decrease, and the amount |  |
| subtracted changes each time in a predictable way. |  |, | a coin with a value of 1 cent or 1/100 of a dollar. |
| :--- |
| Penny |
| Perimeter |
| the distance around a closed two-dimensional figure or shape. In the case of a |
| circle, the distance around is the circumference. ${ }^{63}$ |


| Place value | the concept that the order in which digits are written in the base-10 number <br> system determines the value of that digit. For example, in the number 245, the <br> digit 2 is in the hundreds place, indicating that the value of that particular 2 is <br> actually 2 hundreds or 200. |
| :--- | :--- |
| Plot | to locate a point on a coordinate plane. |
| Plus sign (+) | a symbol (+) that shows that one number is to be added to another. |
| Point | the smallest geometric unit and a figure with no dimensions-it has no length, <br> width, or height. A point is generally indicated with a single dot and is labeled <br> with a single capital letter (e.g., point P). When the point appears at the end of a <br> figure (e.g., a line segment or a ray), it is referred to as an endpoint. |
| Positional words | words that enhance a student's ability to follow and give directions such as, on, <br> off, in, out. |
| Positive number | any number greater than zero or to the right of zero on the number line. |
| Possible | able to be done or achieved; able to exist. |
| Pound (lb) | a customary unit used to measure mass; 1 pound = 16 ounces. |
| Power | a small number written to the right and above a base number signifying how <br> many times the base number is to be multiplied to itself. |
| Precise (Precision) | exact in measuring; accurate. |
| Predict | to use known information in order to make a logical guess as to a future <br> outcome. |
| Prediction | a reasonable guess as to what will happen |
| Probability | the chance that an event will occur. Probabilities can be described as likely, if <br> the event will most probably happen; certain, if the event will definitely happen <br> (a probability equal to 1); impossible, if the event cannot happen or (a <br> probability equal to 0); unlikely, if there is little chance that the event will <br> happen. A probability can also be expressed as a fraction (e.g., 3/12 ). |
| Product | the result when one number is multiplied by one or more numbers; the answer <br> to a multiplication computation. |
| characteristics that are true for a geometric shape in a particular class of |  |
| geometric shapes (e.g., quadrilaterals) |  |


| Properties of operations | concepts and processes that have a pattern of regularity and logical order (e.g., commutative property, associative property, distributive property) |
| :---: | :---: |
| Proportional | having parts that are the correct or appropriate size in relation to each other |
| Putting together | bringing two or more quantities together to make a new total. |
| Quantity | the amount or number of a material or immaterial thing not usually estimated by spatial measurement. |
| Quarter | a coin with a value of 25 cents or $1 / 4$ of a dollar. |
| Quarter hour | a period of 15 minutes. |
| Quotient | the result of a division problem. |
| Rate of change | a ratio that compares change in a dependent variable (i.e., $y$-value) in relation to a change in the independent variable (i.e., $x$-value). |
| Ratio | tells us how much of one thing there is as compared to another thing. Ratios can be written as 3:4, 3 to 4 , or $3 / 4$ ). |
| Read the data | to find information explicitly stated in displays of data (e.g., tables, lists, graphs, etc.), recognizing graphical conventions, and making direct connections between the original data and the display. |
| Real-world problems | the quantitative and spatial problems that arise from a wide variety of human experiences with applications to careers (e.g., making change, figuring sale prices, or comparing payment plans). |
| Recognize | to identify from knowledge of appearance or characteristic; to select from a set of given choices. |
| Rectangle | a polygon with four sides and four right angles, opposite sides are equal and parallel. |
| Rectangular prism | a three-dimensional object constructed from three pairs of parallel rectangles (called faces) that share common edges so as to form an enclosed space such that opposite rectangles are congruent. The vertices of the rectangles are the vertices of the prism, and the sides of the rectangles are called edges. |
| Recursive pattern (rule) | a pattern in which each number is found from the previous number by repeating a process. |


| Reflection | the transformation of a figure that produces the mirror image of the original <br> figure. As a result of the transformation, the line over which the reflection <br> occurs becomes a line of symmetry. Informally, a reflection can be thought of as <br> a "flip" of the original figure. |
| :--- | :--- |
| Regroup | a process of reorganizing numbers using place value; a "trading process" that <br> utilizes the equivalents of 1 hundred for 10 tens or 1 ten for 10 ones, etc. For <br> example, when subtracting 309 from 428,428 is regrouped into 4 hundreds, 1 <br> ten and 18 ones. |
| Relationship | understanding how and why the rules and procedures work. |
| Relative position | a location established with reference to another point. |
| Relative value | a value established with reference to other values. |
| Remainder | the amount left over when one number or polynomial is divided by another <br> number or polynomial. If the remainder is zero, it is usually said that there is no <br> remainder. |
| Remaining | left over, existing. |
| Repeated addition | add equal groups together to find the total, often used to model the concept of <br> multiplication. |
| Repeating pattern | a pattern that is cyclical in nature, with each cycle repeating elements in the <br> same order. |
| Represent (Representations) | the use of symbols, charts, graphs, manipulatives, and diagrams that show <br> mathematical ideas or relationships. |
| Results | solutions; outcomes. |
| Right angle | an angle formed by two perpendicular lines, the measure of which is $90^{\circ}$. |
| Rotation | a type of transformation that moves a figure around a fixed point in a circle, <br> called the center of rotation. |
| Round a number | making a number simpler and easier to use but keeping it close to what it was <br> and understanding that it is less accurate (e.g., rounding to the nearest 10; 73 <br> rounds to 70, 48 rounds to 50). |
| Routine | the usual series of things that are done at a particular time; the practice of <br> regularly doing things in a fixed order. |
|  |  |


| Row | a set of data arranged horizontally. |
| :--- | :--- |
| Rule (for a pattern) | a general statement written in numbers or words that describes how to <br> determine any term in a pattern. Rules or generalizations for patterns may <br> include both recursive and explicit notation. In the recursive form of pattern <br> generalization, the rule focuses on the rate of change from one element to the <br> next. |
| Ruler | a tool used to measure length. |
| Same | identical; not different |
| Second | a unit to measure time; 1 second = 1/60 of a minute. |
| Section | a distinct part or parts into which something is or may be divided or from which <br> it is made up (e.g., sections of a pie chart). |
| Select | carefully choose as being the best or most suitable. |
| Separate | 1. (verb) See: Partition. <br> 2. (adjective) forming or viewed as a unit apart or by itself; not joined or <br> touching physically. |
| Sequence | a sequence, in mathematics, is a string of numbers, that follow a particular <br> pattern. |
| Set model | the use of a discrete set of objects to represent the whole and a subset of those <br> objects to represent a fraction. |
| Sets | a collection of distinct elements or items. |
| Shape | 1. (two-dimensional) a figure that has length and width, but no height (e.g., <br> circle, square, and triangle). <br> 2. (three-dimensional) an object that has three measurable dimensions - length, <br> width, and height (e.g., prism, pyramid, cylinder, and cone). |
| Short (shorter, shortest) | measuring a small distance from end to end; lasting a small amount of <br> time; comparing distance or time. |
| Short hand | the shorter hand on an analog clock; the hand on an analog clock that tells the <br> minutes. |
| Shrinking pattern | patterns in which the numbers decrease, and the amount subtracted changes <br> each time in a predictable way. |


| Side | a straight line segment of a 2-dimensional shape that is "closed" (all the lines <br> connect up). |
| :--- | :--- |
| Similar figures | two or more figures that have the same shape, but not necessarily the same <br> size. |
| Simple ratio | neither number in the ratio has a common factor (i.e., 2:4 is a whole number <br> ratio, but divide both numbers by 2 and you get 1:2 which is a SIMPLE whole <br> number ratio) |
| Size | the relative extent of how big or small something is by dimension, value or <br> magnitude. |
| Skip count | to count by twos, threes, fives, etc., skipping the numbers in between. |
| Slide | a type of transformation that moves every point in a graph or geometric figure <br> by the same distance in the same direction without a change in orientation or <br> size. |
| Small | having comparatively little size or slight dimensions. |
| Solve | to find the answer to an equation or a problem. |
| Sort | to separate objects into groups according to properties or characteristics. |
| Split | the process of dividing shapes or quantities, usually into equal parts. |
| Square | a polygon with four equal sides and four right angles. |
| Square foot (ft ${ }^{2}$ ) | a customary unit of measure for area (1 ft. ${ }^{2}=144$ in. ${ }^{2}$ ). |
| Square root | a number that, when multiplied by itself, yields the original number. For <br> example, 3 squared is 9, so a square root of 9 is 3. |
| Square unit | a unit that has length and width, and is used to measure area (e.g., square <br> inches, square centimeters, acres, etc.). |
| Squared | The product obtained when a number is multiplied by itself (e.g., 3 squared is 9). |
| Standard tools | a type of measurement tool in which exact measurements can be taken (i.e., <br> rules, yardsticks, measuring cups, balance) |
| Standard units of measure | all customary and metric units of measure. |
|  |  |


| Strategies | any method used to carry out a computation, whether a traditional pencil-and- <br> paper algorithm (i.e., method), an informal written or mental strategy, use of <br> objects, or some combination of these methods. A strategy can include <br> instructional methods, such as activities involving number puzzles, number- <br> related games, multiple solution strategies, etc. |
| :--- | :--- |
| Subitize | to judge the number of objects in a group accurately without counting. |
| Subtract | the process of taking one amount from another or finding the difference <br> between two numbers. |
| Subtraction | a mathematical operation that finds the difference between two quantities or <br> how much more one quantity is than a second quantity. |
| Subtraction sign (-) | a symbol (-) that is read as "minus" or "take away" to represent subtraction. |
| Successive term | one after the other |
| Sum | the result when adding two or more numbers (i.e., the answer to an addition <br> computation). |
| Summarize | to give the main points |
| Symbol | a notation used to represent an operation or abstract idea (e.g.,,,$+->$, or $\pi$ ). |
| Symmetry | 1. (symmetric) a geometric figure or graph that consists of two congruent parts. <br> $2 . ~(l i n e ~ s y m m e t r y) ~ o n e ~ s i d e ~ o f ~ a ~ s h a p e ~ i s ~ a ~ m i r r o r ~ i m a g e ~ o f ~ t h e ~ o t h e r ~ s i d e . ~$ |
| Table | a set of data, such as words, numbers, or symbols, organized in rows and <br> columns. |
| Taking away | removing one quantity from another to make a new total. |
| Tall (taller, tallest) | something that has height especially relative to width; compare heights of <br> objects |
| Telling time | keep track of the hours; know how to read a clock or watch |
| Temperature | the extent of warmth or coldness of something; a thermometer is used to <br> measure temperature in Fahrenheit ( ${ }^{\circ}$ F) or Celsius ( ${ }^{\circ} \mathrm{C}$ ). |
| Tens | sets of 10 ones (i.e., $10,20,30,40,50,60,70,80$, or 90$).$ |
| Tens place | the numeral located 2 places to the left of the decimal point; tells how many <br> groups of ten are in the quantity. |
| Tenths | one of 10 equal parts; 1 digit to the right of a decimal point. |


| Tenths place | the place value located 1 place to the right of the decimal point; 1 out of 10 <br> equal parts of a whole. |
| :--- | :--- |
| Thermometer | an instrument used to measure temperature (how hot or cold a thing is), usually <br> in the Celsius or Fahrenheit scale. |
| Thirds | a whole divided into three equal parts. |
| Three-digit number | a whole number greater than 99 and less than 1000. |
| Three-dimensional shape | an object that has three measurable dimensions - length, width, and height <br> (e.g., prism, pyramid, cylinder, and cone). |
| Tiling | Fitting individual tiles together with no gaps or overlaps to fill a flat space. |
| Time | a system of measuring duration or a specific portion of duration (e.g., year, <br> season, day, hour, minute, and second). |
| Times | the processes by which a number is added to itself a specified number of times. |
| Title | a label typically at the top of a graph that tells us what the graph is about. |
| Today | this present day. |
| Tomorrow | the day after today. |
| Tool | any instrument used to solve a problem; it does not necessarily involve <br> technology. |
| Total | the whole amount or the sum. |
| Transformation | the application of a rule that may change the size or location of a geometric <br> figure. Transformations may include translation, reflection, or rotation. |
| Translation | a type of transformation that moves every point in a graph or geometric figure <br> by the same distance in the same direction without a change in orientation or <br> size. |
| Trend | move in a particular direction as in increasing or decreasing. |
| Triangle | a polygon with exactly three sides. A triangle may be classified by its angle <br> measures (i.e., acute triangle, obtuse triangle, or right triangle) |
| TRUE | consistent with fact; accurate; real. |
| Turn | a type of transformation that moves a figure around a fixed point in a circle, <br> called the center of rotation. |
|  |  |


| Two-digit number | a whole number greater than 9 and less than 100. |
| :--- | :--- |
| Two-dimensional shape | a figure that has length and width, but no height (e.g., circle, square, and <br> triangle). |
| Understand | to construct meaning from instructional messages, including oral, written, and <br> graphical communication. |
| Understanding | the ability to apply concepts and categories |
| Unequal | not equal in quantity, size, or value. |
| Unit | a label for a measurement; a single something. |
| Unit cube | a cube whose sides are one unit long. The volume of a three-dimensional unit <br> cube is one cubic unit, and its total surface area is six square units. |
| Unit fraction | a fraction with a numerator of 1, such as 1/4 or 1/3. |
| Unit of capacity | a unit used to measure the amount that can be contained in an object (usually <br> liquid); customary units include cup, pint (pt), quart (qt), and gallon (gal); metric <br> units include liter (L), kiloliter (kL), and milliliter (mL). |
| Unit of measurement (unit of length) | a standard amount or quantity. Common examples are inches (in.), feet (ft), <br> ounces (oz), grams (g), minutes (min), hours (hr), etc. |
| Unit square | a square with each side one unit in length. The area of a unit square is one <br> square unit. |
| Unknown | a numerical value that is not known, often represented by a variable. |
| Unlike denominators | two or more fractions with unequal denominators (e.g.,6/17 and 3/7 ). |
| Value | 1. a numerical quantity; how much something is worth. <br> 2. the possible outcomes of a variable. For example, small, medium, and large <br> are possible values for the variable size. |
| Variability | the degree to which values in a distribution differ. |
| Variable | 1. a quantity that can change or that may take on different values. <br> 2. a symbol (often a letter of the alphabet, sometimes including the Greek <br> alphabet) that represents a number in a mathematical expression (e.g., $x$, a, n, <br> etc.). |
| Vertical axis | the vertical axis of a coordinate grid (y-axis). |
|  |  |


| Visual fraction model | A diagram or representation to show the relative size of a fraction. |
| :---: | :---: |
| Visual representation | creating and forming models that reflect mathematical information |
| Volume | the amount of space in cubic units that a three-dimensional (solid) figure occupies or contains. Units, such as cubic meters $\left(\mathrm{m}^{3}\right)$, cubic inches (in. ${ }^{3}$ ), gallons (g), liters (L), and fluid ounces ( fl oz ) are used to measure volume. |
| Week | a unit used to measure time; one week = seven days. |
| Weight | Heaviness, the effect of gravitational pull on an object. Formal units of weight include pounds (lb), ounces (oz), and kilograms (kg). |
| Whole | 1. the sum in part-part-whole addition problems. <br> 2. a chosen unit in a discussion of fractions. <br> 3. an object that is complete in itself |
| Whole numbers | the numbers $0,1,2,3 \ldots$; the numbers that do not include fractional parts or negative values. |
| Width | the measurement or extent of something from side to side. |
| Word problem | any mathematics exercise expressed as a situation explained in words. |
| X marks | a method of visually displaying a distribution of data values where each data value is shown as a dot or $x$ mark above a number line. Also known as a dot plot. |
| $x$ - and $y$-values | a magnitude, quantity, or number denoted by the algebraic terms $x$ and $y$. |
| $x$-axis | the horizontal axis of a coordinate grid. |
| $x$-coordinate | the horizontal value in a pair of coordinates (i.e., how far along the point is). The $x$-coordinate is always written first in an ordered pair of coordinates $(x, y)$, such as $(12,5)$. In this example, the value 12 is the $x$-coordinate. |
| $y$-axis | the vertical axis of a coordinate grid. ${ }^{63}$ |
| $y$-coordinate | the vertical value in a pair of coordinates (i.e., how far up or down the point is). The $y$-coordinate is always written second in an ordered pair of coordinates ( $x$, $y)$, such as $(12,5)$. In this example, the value 5 is the $y$-coordinate. |
| Yard (yd) | a customary unit used to measure length; one yard = three feet. |
| Yardstick | a graduated measuring stick one yard in length. |
| yesterday | the day before today. |

the number which indicates no quantity, size, or magnitude; zero is neither negative nor positive; zero is the additive identity.

